Preference Aggregation by Voting: Algorithmics and Complexity

Präferenzaggregation durch Wählen: Algorithmik und Komplexität

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Website

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Preference Aggregation by Voting

In **Approval voting**, every voter approves of (gives 1 point to) or disapproves of (gives 0 points to) each candidate. Whoever has the most approvals wins.

- A No election has more than one approval winner
- B Approval voting is a voiced voting system
- C Approval voting satisfies Unique-WARP
- D Approval voting is susceptible to constructive control by adding candidates

Question 2

Is it possible to partition $V = \{v_1, ..., v_{10}\}$ into V_1 and V_2 such that when in the TP model the approval winners of (C, V_1) and (C, V_2) run against each other, c is not the unique approval winner?

A Yes, with $V_1 = \{v_1, \dots, v_7\}$ and $V_2 = \{v_8, v_9, v_{10}\}$

B No

- C Yes, with $V_1 = \{v_1, v_2, v_5, v_6, v_7\}$ and $V_2 = \{v_3, v_4, v_8, v_9, v_{10}\}$
- D Yes, with $V_1 = \{v_1, v_2, v_3, v_5, v_6, v_7\}$ and $V_2 = \{v_4, v_8, v_9, v_{10}\}$

Question 3

 $\begin{array}{c|cccc} a & b & c \\ \hline v_1, \dots, v_4 & 0 & 0 & 1 \\ \hline v_5, v_6, v_7 & 1 & 0 & 0 \\ \hline v_8, v_9, v_{10} & 0 & 1 & 0 \end{array}$

Is it possible to partition $V = \{v_1, ..., v_{10}\}$ into V_1 and V_2 such that when in the TE model the approval winners of (C, V_1) and (C, V_2) run against each other, c is not the unique approval winner?

A Yes, with $V_1 = \{v_1, \dots, v_7\}$ and $V_2 = \{v_8, v_9, v_{10}\}$

B No

- C Yes, with $V_1 = \{v_1, v_2, v_5, v_6, v_7\}$ and $V_2 = \{v_3, v_4, v_8, v_9, v_{10}\}$
- D Yes, with $V_1 = \{v_1, v_2, v_3, v_5, v_6, v_7\}$ and $V_2 = \{v_4, v_8, v_9, v_{10}\}$

Question 4

 $\begin{array}{cccc} & a & b & c \\ \hline v_1, v_2, v_3: & 1 & 0 & 0 \\ \hline v_4, v_5: & 0 & 1 & 0 \\ \hline v_6, v_7, v_8: & 0 & 0 & 1 \end{array}$

Is it possible to partition $V = \{v_1, ..., v_8\}$ into V_1 and V_2 such that when in the TP model the approval winners of (C, V_1) and (C, V_2) run against each other, c is the unique approval winner?

A Yes, with $V_1 = \{v_1, ..., v_4\}$ and $V_2 = \{v_5, ..., v_8\}$

B No

- C Yes, with $V_1 = \{v_1, v_3, v_5, v_7\}$ and $V_2 = \{v_2, v_4, v_6, v_8\}$
- D Yes, with $V_1 = \{v_1, v_2, v_6, v_7, v_8\}$ and $V_2 = \{v_3, v_4, v_5\}$

Question 5

 $\begin{array}{ccccc} & a & b & c \\ v_1, v_2, v_3 & & 1 & 0 & 0 \\ v_4, v_5 & & 0 & 1 & 0 \\ v_6, v_7, v_8 & & 0 & 0 & 1 \end{array}$

Is it possible to partition $V = \{v_1, ..., v_8\}$ into V_1 and V_2 such that when in the TE model the approval winners of (C, V_1) and (C, V_2) run against each other, c is the unique approval winner?

- A Yes, with $V_1 = \{v_1, ..., v_4\}$ and $V_2 = \{v_5, ..., v_8\}$
- B No
- C Yes, with $V_1 = \{v_1, v_3, v_5, v_7\}$ and $V_2 = \{v_2, v_4, v_6, v_8\}$
- D Yes, with $V_1 = \{v_1, v_2, v_6, v_7, v_8\}$ and $V_2 = \{v_3, v_4, v_5\}$

Suppose *c* is the distinguished candidate in an election (C, V). In which of the following control scenarios is it allowed and can it make sense to delete *c*?

- A CCAC
- **B** DCAC
- C CCDC
- D DCDC

Suppose *c* is the distinguished candidate in an approval election (C, V). In which of the following control scenarios is it allowed and can it make sense to do the given action?

- A CCDC: delete the strongest rival of c
- B DCDC: delete the strongest rival of c
- C CCPC-TE: partition C into $C_1 = \{c\}$ and $C_2 = C \setminus \{c\}$
- D DCPC-TE: partition *C* into $C_1 = \{c\}$ and $C_2 = C \setminus \{c\}$

Your preferences when the pandemic will end are:

2022	2023	never	2024
2024	2022	never	2023
2023	2024	never	2022
2024	2022	never	2023
2023	2022	never	2024

Which of the following voting rules should we use?

- A Plurality
- B Veto
- C Borda
- D Condorcet

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