### Algorithmic Game Theory Algorithmische Spieltheorie Pingo Wintersemester 2022/2023

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Pingo

## Access Number: 885317



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#### Question 1

Let G = (P, v) be a nonmonotonic cooperative game with *n* players. Consider the payoff vector ( $\varphi_1(G), \ldots, \varphi_n(G)$ ). Which of the following statements are true?

A 
$$\sum_{i=1}^{n} \varphi_i(G) = v(P).$$

B If  $\varphi_i(G) = 0$  then  $i \in P$  is a dummy player.

**C**  $\varphi_i(G) = \varphi_i(G)$  for symmetric players *i* and *j*.

 $\mathsf{D} \varphi_i(G+G) = 2\varphi_i(G).$ 

Does adding players to a weighted voting game necessarily decrease the power (in terms of their Shapley–Shubik index) of the originally existing players?

A Yes.

B No.

Suppose a player in a weighted voting game splits into several identities ("false-name manipulation"). Is it possible that these new players together have a total power (in terms of the sum of their Shapley–Shubik indices) that is higher than the original player's power?

- A Yes.
- B No.

Suppose a player in a weighted voting game splits into several identities ("false-name manipulation"). Is it possible that these new players together have a total power (in terms of the sum of their Shapley–Shubik indices) that is lower than the original player's power?

A Yes.

B No.

Consider the weighted voting game G = (4, 4, 1, 1; q).

How would you choose the quota *q* to make sure that each of the weight-1 players has the same total power (in terms of the Shapley–Shubik index) as any of the weight-4 players?

- A q = 5.
- **B** *q* = 8.
- **C** *q* = 10.